Errata (September 5, 2013)

$$\begin{array}{l} \underline{\mathbf{p}. \ 42, \ \lim 3 \downarrow} \\ \hline C_e^*(K) = \cdots = e^{-rT} \int_K^\infty (x - K) \varphi_T^*(x) \, dx \\ \underline{\mathbf{p}. \ 65, \ \lim 1 \downarrow} \\ \hline \dots \ \varphi_1, \varphi_2 \in \mathbb{R}^{d+1} \dots \\ \underline{\mathbf{p}. \ 106, \ \lim 5 \downarrow} \\ \hline \dots \ for \ |h| > 0 \dots \\ \underline{\mathbf{p}. \ 115, \ \lim 2 \downarrow} \\ \hline \psi(L) = \sum_{i=0}^\infty \psi_i L^i \\ \underline{\mathbf{p}. \ 118, \ \lim 4 \uparrow} \\ \hline \dots \ if \ |z_j| > 1 \dots \\ \underline{\mathbf{p}. \ 148, \ \lim 10 \uparrow} \\ \hline \dots \ from \ time \ t - 1 \ to \ t \ \dots \\ \underline{\mathbf{p}. \ 154, \ Definition \ 4.4.2} \\ \hline \dots \ if \ there \ is \ some \ self-financing \ trading \ strategy... \\ \underline{\mathbf{p}. \ 156, \ \lim 11 \downarrow} \\ \hline Thus, \ 1_{\Omega \setminus A_c} \cdot E^*(V_t^* | \mathcal{F}_t) + 1_{A_c} V_{t-1}^* \ is \ a \ version \ of \ E(V_t^* | \mathcal{F}_{t-1}). \\ \mathbf{p}. \ 158, \ Theorem \ 4.4.8 \end{array}$$

In the proof of Theorem 4.4.8 the definition of \mathcal{V} is not correct (one considers the discounted terminal values but has to allow for self-financing strategies) and it is instructive to add the details of the verification that \widetilde{Q} is an equivalent martingale measure, which are similar to the argument in Theorem 4.3.5. Here are the changes:

Define

$$\mathcal{V} = \left\{ V_0 + \int_0^T \varphi_t' \, dS_t^*, \quad \{\varphi_t\} \text{ predictable}, V_0 \text{ a constant} \right\}$$

In order to verify that S_t^* is a \mathcal{F}_t -martingale under \widetilde{Q} , it suffices to show that

$$E_{\widetilde{Q}}\left(\int_{0}^{T}\varphi_{t}^{\prime}\,dS_{t}^{*}\right) = 0 \tag{1}$$

for all predictable and bounded $\{\varphi_t\}$. Indeed, this implies that

$$E_{\widetilde{Q}}\left(1_A(S^*_{t+1,i}-S^*_{t,i})\right) = 0, \qquad A \in \mathcal{F}_t,$$

which is equivalent to $E_{\widetilde{Q}}(S^*_{t+1,i}|\mathcal{F}_t) = S^*_{t,i}$, since the left-hand side equals $\int_0^T \varphi'_t dS^*_t$, if we put $\varphi_{uj} = 1_A$ if u = t and j = i and $\varphi_{uj} = 0$ otherwise. To check (1), notice that by definition of Q

$$E_{\widetilde{Q}}\left(\int_0^T \varphi_t' \, dS_t^*\right) = E^*\left(\int_0^T \varphi_t' \, dS_t^*\right) + \frac{1}{\|C_{\mathcal{V}^\perp}\|_{\infty}} \int C_{\mathcal{V}^\perp}^* \int \varphi_t' \, dS_t^* \, dP^*.$$

The first term vanishes, since φ_t is predictable and S_t^* a martingale under P^* . The second one can is given as $\frac{1}{\|C_{\mathcal{V}^{\perp}}\|_{\infty}}(C_{\mathcal{V}^{\perp}}^*, \int \varphi'_t \, dS_t^*) = 0$, since $\int \varphi'_t \, dS_t^* \in \mathcal{V}$. p. 159, line $3 \uparrow$ p.

$$\frac{159, \text{ line } 3\uparrow}{\dots E(C^*|\mathcal{F}_t)\dots}$$

p. 161, line 8 \downarrow

The model is arbitrage-free if and only if $\mathcal{P} = \{P^*\}$. Then S_t^* is a martingale under P^* and...

p. 167, line 3 ↓
Replace
$$\sigma/\sqrt{n}$$
 by σ .
p. 167, line 9 ↑
Replace $B(1)$ by B_1 .
p. 320, line 6 ↑
Replace m^2/T by m^3/T .

p. 322, line 3,5 \uparrow Replace $\frac{1}{N}|$ in front of $|\sum ...|$ by $\frac{1}{T}$. The final estimate is $O(m^3/T)$ instead of $O(m^2/T)$.

p. 352, line 9
$$\uparrow$$

Replace dx_t by dx_T .

p. 352, Theorem 9.3.2

The proof is written down for a non-randomized test δ . Replacing (at lines 9,15) $P_0(\delta = 1)$ by $E_0(\delta)$ and $P_k(\delta = 1)$ by $E_k(\delta)$ (at line 2) and deleting $= P_k(\delta = 1)$ (at line 11) yields the proof for a randomized test δ . p. 354, line 10 \downarrow

Replace $L_1(X_1, \ldots, X_T)$ by $L_0(X_1, \ldots, X_T)$.

<u>p. 360, line 9 \downarrow </u>

Delete the first $\frac{1}{\sqrt{T}}$ in front of \widehat{m}_t .